

KLASSIK MEXANIKANING MURAKKAB HODISALARINI PYTHON ANIMATSIYALARI ORQALI VIZUALLASHTIRISH

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Annotatsiya

Maqola fizik hodisalarni o'qishni soddalashtirishda Python animatsiyalarining roli haqida. Klassik mexanikaning ikkita asosiy masalasi (mayatnik va snaryad harakati) SciPy, NumPy va Matplotlib kutubxonalarini orqali vizuallashtirilib, har bir animatsiya kodining fizik va matematikasini tushuntirildi. Runge-Kutta va Eyer usullari amaliy misollar bilan ko'rsatildi. Maqola fizika o'qituvchilari va Python programmalarini o'rganayotgan talabalar uchun foydalidir.

Kalit so'zlar: Python animatsiya, vizualizatsiya, differensial tenglamalar, klassik mexanika, ta'lim texnologiyasi.

Fizika — bu tabiat qonuniyatlarini o'rganadigan fan bo'lsa, dasturlash — bu qonuniyatlarni raqamli dunyoda jonlantirish vositasidir. Python o'zining sodda sintaksisi va boy kutubxonalarini bilan murakkab fizik jarayonlarni vizuallashtirish uchun eng qulay tildir. Fizikadagi murakkab hodisalarni animatsiyalar orqali tushuntirish ancha samarali va qiziqarli qiladi. Bu

animatsiyalarda Python dan foydalanish esa har bir xususiy holat uchun yangi animatsiyalarni oson yaratishga yordam beradi. Ushbu maqolada biz **Mayatnik harakati**, **Snaryad harakati** Python yordamida animatsiya qilamiz.

Barcha animatsiyalar uchun biz asosan uchta kutubxonadan foydalanamiz:

NumPy — Matematik hisob-kitoblar uchun

Matplotlib — Grafik va animatsiya uchun

SciPy — Differensial tenglamalarni yechish uchun Birinchi navbatda mayatnik harakatini ko'rib chiqsak:

pendulum_ode funksiyasi — Bu funksiya ikkinchi tartibli differensial tenglamani birinchi tartibli sistema ko'rinishiga o'tkazadi. Matematikada bu standart usul: bir o'zgaruvchi (θ) o'rniga ikkitasini (θ va ω) kuzatamiz.

solve_ivp — SciPy kutubxonasidan olingan bu funksiya differensial tenglamalarni Runge-Kutta usulida yechadi. $rtol=1e-8$ parametri hisoblash aniqligini oshiradi — fizik tajribalarda aniqlik muhim.

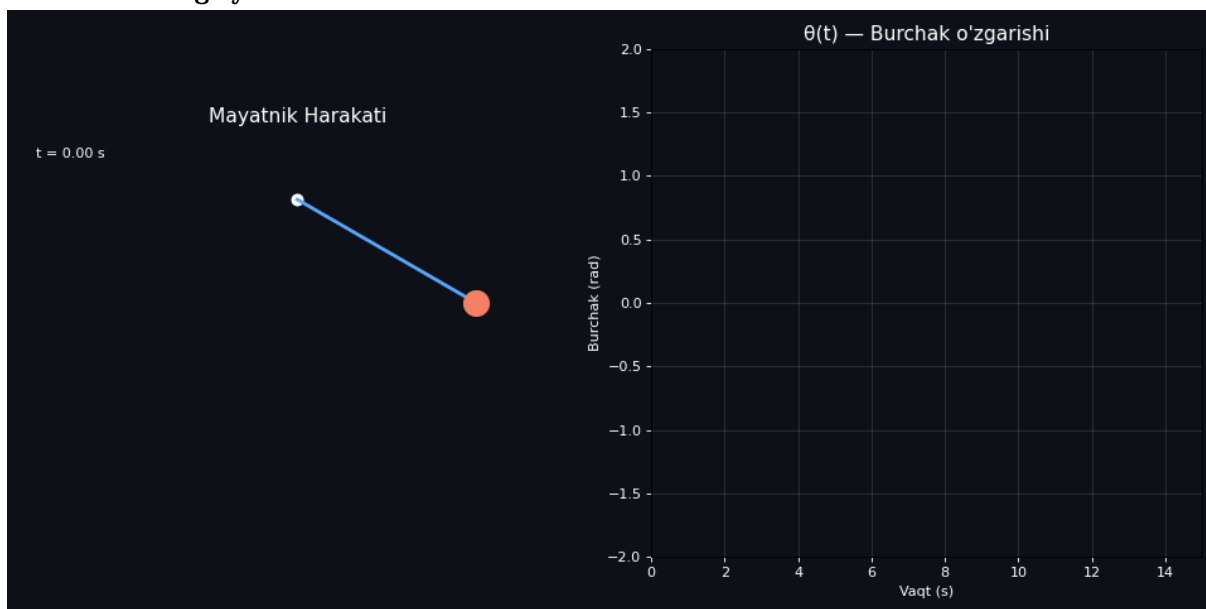
FuncAnimation — Matplotlib-ning animatsiya mexanizmi. Har bir frame uchun animate funksiyasi chaqiriladi va grafik elementlari yangilanadi. $blit=True$ faqat o'zgaragan qismlarni qayta chizadi — bu tezlikni oshiradi.

```

1 import numpy as np
2 import matplotlib.pyplot as plt
3 import matplotlib.animation as animation
4 from scipy.integrate import solve_ivp
5
6 # =====
7 # 1-QISM: MAYATNIK
8 # =====
9 g = 9.81
10 L = 1.5
11 theta0 = np.pi / 3
12 omega0 = 0.8
13
14 def pendulum_ode(t, y):
15     theta, omega = y
16     return [omega, -(g / L) * np.sin(theta)]
17
18 t_eval = np.linspace(0, 15, 5500)
19 solution = solve_ivp(pendulum_ode, (0, 15), [theta0, omega0],
20                     t_eval=t_eval, method='RK45', rtol=1e-8)
21 theta = solution.y[0]
22 x_bob = L * np.sin(theta)
23 y_bob = -L * np.cos(theta)
24
25 fig1, (ax1, ax2) = plt.subplots(1, 2, figsize=(12, 6))
26 fig1.patch.set_facecolor('k')
27
28 ax1.set_xlim(-2, 2); ax1.set_ylim(-2, 0.5)
29 ax1.set_aspect('equal'); ax1.set_facecolor('k')
30 ax1.set_title("Mayatnik Harakati", color='white', fontsize=14)
31 ax1.axis('off')
32
33 ax2.set_xlim(0, 15); ax2.set_ylim(-2, 2)
34 ax2.set_facecolor('k')
35 ax2.set_title("θ(t) — Burchak o'zgarishi", color='white', fontsize=14)
36 ax2.set_xlabel("vaqt (s)", color='white')
37 ax2.set_ylabel("Burchak (rad)", color='white')
38 ax2.tick_params(color='white')
39 ax2.grid(True, alpha=0.2)
40
41 ax1.plot(0, 0, 'o', color='white', markersize=8)
42 rd_line = ax1.plot([], [], '-', color='r', linewidth=2.5)
43 bob_circle = ax1.plot([], [], 'o', color='r', markersize=18)
44 trace_line = ax1.plot([], [], '-', color='r', alpha=0.3, linewidth=1)
45 time_text = ax1.text(-1.5, 0.3, '', color='white', fontsize=10)
46 graph_line = ax2.plot([], [], '-', color='r', linewidth=1.5)
47
48 trace_x, trace_y = [], []
49
50 def animate1(frame):
51     i = min(frame * 3, len(x_bob) - 1)
52     rd_line.set_data([x_bob[i], y_bob[i]])
53     bob_circle.set_data(x_bob[i], y_bob[i])
54     trace_x.append(x_bob[i]); trace_y.append(y_bob[i])
55     if len(trace_x) > 8:
56         trace_x.pop(0); trace_y.pop(0)
57     trace_line.set_data(trace_x, trace_y)
58     time_text.set_text(f"t = {x_bob[i]:.2f} s")
59     graph_line.set_data(t_eval[:i], theta[:i])
60     return rd_line, bob_circle, trace_line, time_text, graph_line
61
62 anim1 = animation.FuncAnimation(fig1, animate1, frames=500, interval=30, blit=True)
63 plt.tight_layout()
64 anim1.save("mayatnik_animatsiya.gif", writer='pillow', fps=30, dpi=80)
65 print("mayatnik_animatsiya.gif saqlandi")
66 plt.close()

```

Bu animatsiya vaqt o'tishi bilan mayatnik parametrlari o'zgarishini mayatnik harakati va diagramma orqali tushuntirilgan. Bu animatsiya orqali jarayonni tushuntirish formulalarni real ko'z bilan ko'rishga yordam beradi.



Snaryad harakati

Snaryad (proektily) harakati — ikki o'lchovli kinematikaning klassik misoli. Bu harakatlarni havoning qarshilik kuchi bor va havo qarshilik kuchi mavjud bo'lmagan holatini ko'rib chiqamiz.

Eyler usuli — compute_trajectory funksiyasida biz sodda lekin samarali Eyler integratsiyasidan foydalanamiz. Har bir dt qadamda tezlik va pozitsiyani yangilaymiz. dt = 0.01 s — bu hisoblash va aniqlik o'rtasidagi muvozanat.

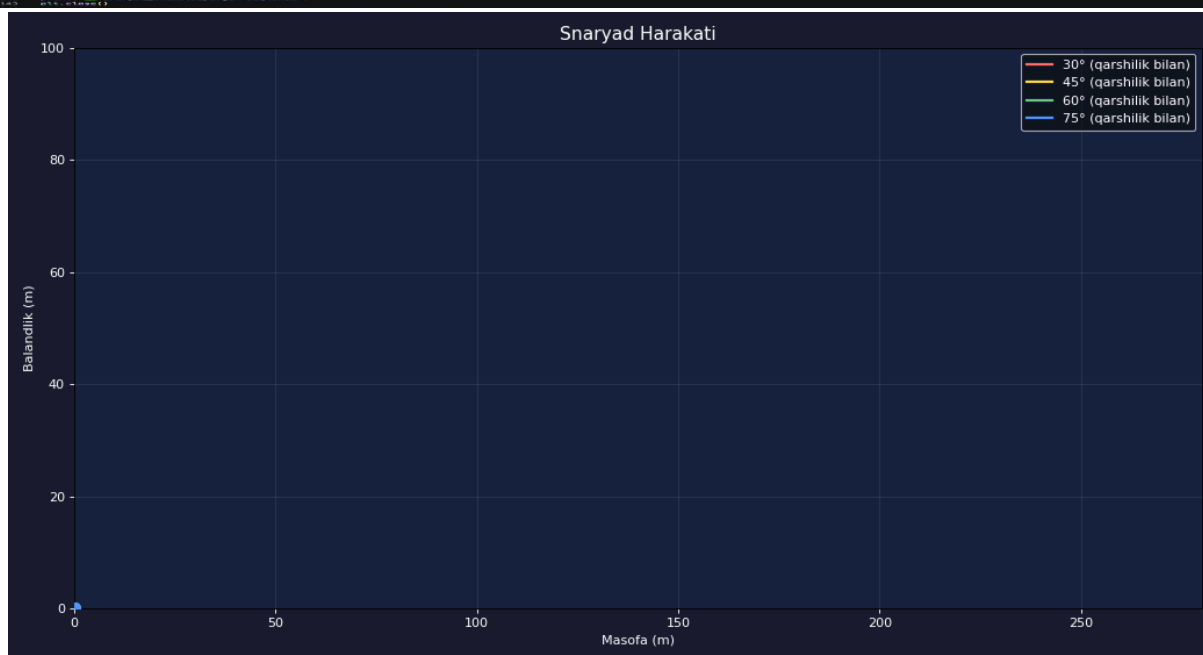
Koeffitsient $k = 0.02$ — mis to'p uchun taxminiy qiymat.

Ikki chiziq — Har bir burchak uchun ikkita traektoriya ko'rsatiladi: real (havo qarshiligi bilan) va ideal. Bu fizikaning muhim tushunchasini vizual ko'rsatadi: havo qarshiligi nafaqat masofani kamaytiradi, balki optimal burchakni ham 45° dan past tomonga siljitadi.

```

1: # -*- coding: utf-8 -*-
2: """
3:     Snaryad harakati
4:     """
5:
6:     import numpy as np
7:     import matplotlib.pyplot as plt
8:     from scipy.integrate import odeint
9:
10:    # Parametrlar
11:    g = 9.81 # m/s^2
12:    k = 0.02 # 1/m
13:    v0 = 100 # m/s
14:    theta = np.radians(30) # 30 degrees
15:
16:    # Bosh shartlar
17:    x0 = 0
18:    y0 = 0
19:    vx0 = v0 * np.cos(theta)
20:    vy0 = v0 * np.sin(theta)
21:
22:    # ODEni yechish
23:    def equations(state, t):
24:        x, y, vx, vy = state
25:        ax = -k * vx
26:        ay = -g - k * vy
27:        return [vx, vy, ax, ay]
28:
29:    state0 = [x0, y0, vx0, vy0]
30:    tspan = [0, 10]
31:    state = odeint(equations, state0, tspan)
32:
33:    # Ideal traektoriya
34:    x_ideal = vx0 * tspan
35:    y_ideal = vy0 * tspan - 0.5 * g * tspan**2
36:
37:    # Vizualizatsiya
38:    plt.plot(x_ideal, y_ideal, 'r--', label='30° (qarshilik bilan)')
39:    plt.plot(x_ideal, y_ideal, 'b--', label='45° (qarshilik bilan)')
40:    plt.plot(x_ideal, y_ideal, 'g--', label='60° (qarshilik bilan)')
41:    plt.plot(x_ideal, y_ideal, 'm--', label='75° (qarshilik bilan)')
42:
43:    plt.xlabel('Masofa (m)')
44:    plt.ylabel('Balandlik (m)')
45:    plt.grid(True)
46:
47:    # O'qish
48:    plt.show()
49:
50:    """
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99:    """
100: """

```



Ushbu maqolada biz Python dasturlash tilining **NumPy**, **Matplotlib** va **SciPy** kutubxonalaridan foydalanib, klassik fizikaning ikkita muhim hodisasini animatsiyalar orqali vizuallashtirdik. Python orqali fizikani animatsiya qilish — nafaqat ta'limning samarali vositasi, balki hozirgi yosh fizikani murakkab jarayonlarni tezda modellashtirish va tajriba qilish imkonini beradi.

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